

# Gapless Spin Excitations in the Kagome- and Triangular-Lattice Antiferromagnets

Hiroki NAKANO<sup>1,2</sup>, Toru SAKAI<sup>1,2,3</sup>,

<sup>1</sup>*Graduate School of Material Science, University of Hyogo, Hyogo, Japan*

<sup>2</sup>*Research Center for New Functional Materials, University of Hyogo, Hyogo, Japan*

<sup>3</sup>*AJapan Agency for Quantum and Radiological Science and Technology (QST), SPring-8, Hyogo, Japan*

The  $S=1/2$  kagome-lattice antiferromagnet is one of interesting frustrated quantum spin systems. The systems exhibit the quantum spin liquid behavior, which was proposed as an origin of the high- $T_c$  superconductivity. The spin gap is an important physical quantity to characterize the spin liquid behavior. Whether the  $S=1/2$  kagome-lattice antiferromagnet is gapless or has a finite spin gap, is still unsolved issue. Because any recently developed numerical calculation methods are not enough to determine it in the thermodynamic limit. Our large-scale numerical diagonalization up to 42-spin clusters and a finite-size scaling analysis indicated that the  $S=1/2$  kagome-lattice antiferromagnet is gapless in the thermodynamic limit[1]. It is consistent with the  $U(1)$  Dirac spin liquid theory of the kagome-lattice antiferromagnet[2,3]. On the other hand, some density matrix renormalization group (DMRG) calculations supported the gapped  $Z_2$  topological spin liquid theory[4,5]. Our recent numerical diagonalization analysis on the magnetization process of a distorted kagome-lattice antiferromagnet indicated that the perfect kagome-lattice system is just on a quantum critical point[6]. It would be a possible reason why it is difficult to determine whether the perfect kagome-lattice antiferromagnet is gapless or gapped.

We propose one of better methods to determine whether the spin excitation is gapless or gapped, based on the finite-size scaling analysis of the spin susceptibility calculated by the numerical diagonalization. The present analysis indicates that the kagome-lattice antiferromagnet is gapless. In order to justify the validity of the method, we try a demonstration for the triangular-lattice antiferromagnet. It confirms the gapless behavior of the triangular-lattice antiferromagnet, as already well known. It suggests that the present method is useful even for such frustrated systems.

The magnetization process of the kagome- and triangular-lattice antiferromagnets will be also discussed[7,8].

[1]H. Nakano and T. Sakai, *J. Phys. Soc. Jpn.*, **2011**, 80, 053704

[2]Y. Ran, M. Hermele, P. A. Lee and X. -G. Wen, *Phys. Rev. Lett.*, **2007**, 98, 117205.

[3]Y. Iqbal, F. Becca, S. Sorella and D. Poilblanc, *Phys. Rev. B*, **2013**, 87, 060405(R).

[4]S. Yan, D. A. Huse and S. R. White, *Science*, **2011**, 332, 1173.

[5]S. Nishimoto, N. Shibata and C. Hotta, *Nature Commun.*, **2013**, 4, 2287.

[6]H. Nakano and T. Sakai, *J. Phys. Soc. Jpn.*, **2014**, 83, 04710.

[7]H. Nakano and T. Sakai, *J. Phys. Soc. Jpn.*, **2015**, 84, 063705.

[8]T. Sakai and H. Nakano, *Phys. Rev. B*, **2011**, 83, 100405(R).