

Frankfurt, April 29, 2015

Exercise Set 2

(Due date: Monday, May 16, 2015)

Exercise 2 (DFT calculation and tight binding fit) (10 points)

Linarite $[\text{PbCuSO}_4(\text{OH})_2]$ is a magnetically ordered insulator. It crystallizes in the monoclinic space group $\text{P2}_1/\text{m}$ (No. 11) with lattice parameters $a = 9.682 \text{ \AA}$, $b = 5.646 \text{ \AA}$, $c = 4.683 \text{ \AA}$, $\alpha = \gamma = 90^\circ$ and $\beta = 102.65^\circ$. The Wyckoff positions are:

Atom	x	y	z		red. coord.	FPLO coord.
Pb	0.34162	0.25	0.32922			
Cu	0	0	0			
S	0.66924	0.25	0.11596			
O1	0.52562	0.25	0.93314	D	$(0, 1/2, 1/2)$	$(0.23202, 0.85742, 1.03374)$
O2	0.66352	0.25	0.42794	B	$(0, 0, 1/2)$	$(0.23202, 0, 1.03374)$
O3	0.25351	0.53644	0.94203	Z	$(0, 1/2, 0)$	$(0, 0.85742, 0)$
O4	0.96662	0.25	0.71304	Y	$(1/2, 0, 0)$	$(0.51244, 0, 0)$
O5	0.09532	0.25	0.26983			
H1	0.86674	0.25	0.61668			
H2	0.05864	0.25	0.45377			

- Compose the cif file for linarite and visualize it (for example using VESTA).
- Prepare an FPLO (Full-potential local-orbital minimum basis code) input file and calculate the bandstructure on the path $\text{D} - \text{B} - \Gamma - \text{Z} - \text{D} - \Gamma - \text{Y}$. Find the main orbital character of the two bands crossing the Fermi level.

Remark: The location of these \mathbf{k} -points in reduced and FPLO coordinates is different. Both notations are given in the above table. In some monoclinic space groups the labelling of high-symmetry points can be different from what one would expect.

- Write a program that fits the two bands crossing the Fermi level with a TB dispersion using an onsite energy and four hopping parameters t_i , $i = 1, 2, 3, 4$. Suitable optimization methods can be found in the `scipy.optimize` module of the Python programming language.
- Calculate the density of states (DOS) from the DFT code.
- Calculate the DOS for the tight binding Hamiltonian and compare it to the one calculated from the DFT code.