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Exercises for Computational Methods in Solid State Theory SS 2014

Exercise Set 1 (Due date: Monday, April 28, 2014)

Exercise 1 (Tight binding and tetrahedron method) (10 points)

Consider a lattice with lattice constants

 $a = 8.5381 \text{\AA}, \quad b = 13.273 \text{\AA}, \quad c = 15.912 \text{\AA}, \quad \alpha = 113.917^{\circ}, \quad \beta = \gamma = 90^{\circ}.$

There are two lattice sites in the positions

$$\vec{\mathbf{s}}_1 = (0, 1/4, 0), \qquad \vec{\mathbf{s}}_2 = (1/2, 3/4, 0).$$

This is an anisotropic triangular lattice with the tight binding Hamiltonian

(1)
$$H = \mu \sum_{i} c_{i}^{\dagger} c_{i} + \sum_{\langle ij \rangle} t(c_{i}^{\dagger} c_{j} + \text{H.c.}) + \sum_{[ij]} t'(c_{i}^{\dagger} c_{j} + \text{H.c.})$$

where $\langle ij \rangle$ and [ij] indicate summations over nearest and next-nearest neighbors, respectively. The nearest neighbour hopping is t = 0.04957735 eV (associated to the distance d = 7.891 Å) and the next nearest neighbour hopping is t' = 0.0426178 eV (associated to the distance d = 8.5381 Å). The chemical potential is $\mu = 0$.

<u>Remark</u>: This model Hamiltonian is obtained from the charge transfer salt κ -(BEDT-TTF)₂Cu₂(CN)₃ at T = 20 K.

a) Write a program that calculates the bandstructure along the path

$$M - X - \Gamma - Y - M - \Gamma$$

in the Brillouin zone where $\Gamma = (0, 0, 0)$, X = (1, 0, 0), Y = (0, 1, 0), and M = (1, 1, 0) in reduced coordinates. Plot the bandstructure, taking into account the different lengths of the path segments in reciprocal space. If you are unsure how the lattice sites are connected by the hoppings, make a sketch.

b) Use the tetrahedron method to calculate the density of states (DOS) for the same tight binding Hamiltonian. Make sure that the DOS is properly normalized. Compare to the result of a brute force calculation of the DOS.

<u>Remark</u>: Please do not write parameters directly into the code. The program is intended for reuse and should be as general as possible.